EMISSION MECHANISMS LESSON 1

CHIARA FERRARI

REFERENCE TEXT:

"ASTROPHYSICAL PROCESSES" BY H. BRADT CAMBRIDGE UNIVERSITY PRESS (2008)







OUTLINE OF THIS LESSON

Overview of this part of the "Cosmology" course

- i. Emission mechanisms
- ii. Astrophysical examples

Thermal bremsstrahlung radiation (with a general introduction)

- i. Measurable quantities in astrophysics
- ii. Thermal bremsstrahlung from a hot plasma of ionized atoms

EMISSION MECHANISMS



Saturday, October 5, 2013

EMISSION MECHANISMS



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Multi-wavelength emission

▶ from galaxies ...

▶ ... and from galaxy clusters



DISCOVERY OF GALAXIES & GALAXY CLUSTERS



XVIII century: Messier and Herschel note the existence of *"nebulae"* and concentrations of them in the sky

<u>1901:</u> Wolf produce the first map of visible light distribution in a cluster of nebulae (Coma)





1920: "Great debate" by Curtis & Shapley

THE ANDROMEDA GALAXY



Saturday, October 5, 2013



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1923: OUR GALAXY IS NOT UNIQUE!



plaque 335 du 6 Octobre 1923 de E Hubble au télescope Hooker de 100° du Mont Wilson, il trouve des "nova" dans M31 mais une (coin haut à droite) est particulière, c'est une céphéide, il remplace le N par VAR (Variable) on va pouvoir ainsi mesurer la distance de M31 document Mont Wilson

THE MASS OF GALAXIES & GALAXY CLUSTERS



NOT ONLY VISIBLE LIGHT: NOT ONLY STARS AND GALAXIES...



Multi-wavelength emission

▶ from galaxies ...

... and from galaxy clusters



Multi-wavelength emission

▶ from galaxies ...

 \triangleright ... and from galaxy clusters



Multi-wavelength emission

▶ from galaxies ...

▶ ... and from galaxy clusters



Multi-wavelength emission

▶ from galaxies ...

▶ ... and from galaxy clusters



DARK MATTER: STILL AN OPEN ISSUE... ...AND NOT EVEN THE BIGGEST ONE!



2011: Nobel in Physics goes to Perlmutter (U.S.), Schimdt (AUS) & Riess (U.S.)



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GENERAL INTRODUCTION MEASURABLE QUANTITIES IN ASTROPHYSICS

Luminosity :

$$L = \int_{SV} j \, dV = \int_0^\infty L(\nu) d\nu$$

- L = total or absolute luminosity (W)
- $L(\nu) = \text{monochromatic luminosity (W Hz}^{-1})$
- SV = source volume
- j = total power radiated per unit volume (W/m³)



▷ Spectral flux density: $S(\nu) = L(\nu)/(4\pi R^2) = \int \int I(\nu, T) d\Omega$

$$S(\nu) = \text{spectral flux density (W m}^{-2} \text{ Hz}^{-1})$$

- $L(\nu) = \text{monochromatic luminosity (W Hz}^{-1})$
- R =source distance
- $I(\nu, T) = \text{specific intensity (W m}^{-2} \text{ Hz}^{-1} \text{ sr}^{-1})$
- $d\Omega = increment \text{ solid angle}$



ANGULAR RESOLUTION





Very Large Array (U.S.)

$Res \propto D^{-1}$

$\leftarrow D \rightarrow$

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RESOLVED & UNRESOLVED SOURCES





 $S(\nu) = L(\nu)/(4\pi R^2) = \int \int I(\nu,T) \mathrm{d}\Omega$

 $S(\nu) = \text{spectral flux density (W m}^{-2} \text{Hz}^{-1})$ $L(\nu) = \text{monochromatic luminosity (W Hz}^{-1})$ R = source distance $I(\nu, T) = \text{specific intensity (W m}^{-2} \text{Hz}^{-1} \text{ sr}^{-1})$ $d\Omega = \text{increment solid angle}$

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STATES OF MATTER



THERMAL BREMSSTRAHLUNG INTRODUCTION: HOT PLASMA

- Gas of charged ions and electrons
- Quasi-neutral over a large volume
- Fourth state of matter
- ▶ Ionization if gas:
 - very hot → collisions between atoms sufficiently strong to remove electrons
 - very rarefied → electrons hardly encounter an ion with which to recombine
 - subjected to an external source of energy → strong electric fields or radiation





Photo-ionization Star forming regions



Collisional ionization Intra-cluster medium



Saturday, October 5, 2013

THERMAL BREMSSTRAHLUNG HOW WE WILL DERIVE THE FINAL EQUATIONS

THERMAL BREMSSTRAHLUNG - PART I COLLISION OF AN ELECTRON WITH AN ION

THERMAL BREMSSTRAHLUNG - PART II COLLISION OF THERMAL ELECTRONS WITH AN ION

THERMAL BREMSSTRAHLUNG - PART III COLLISION OF THERMAL ELECTRONS WITH IONS



$$\mathbf{E}(\mathbf{r},t) = E_{tr}\mathbf{\hat{n}} = \frac{qa(t')sin\theta}{4\pi\epsilon_0 c^2 r}\mathbf{\hat{n}}$$

 $\mathbf{E}(\mathbf{r}, t) =$ Transverse electric vector; V/m; v << c

 $\epsilon_0 E^2/2 = {\rm energy}$ density of electric field $B^2/2\mu_0 = {\rm energy} \ {\rm density} \ {\rm of} \ {\rm magnetic} \ {\rm field}$ B=E/c

$$c^2 = 1/\mu_0\epsilon_0$$

 $\mu_0 = 4\pi \times 10^{-7} \text{ T m A}^{-1} = \text{permeability of free space}$ $\epsilon_0 = 8.854 \times 10^{-12} \text{ s}^4 \text{ A}^2 \text{ m}^{-3} \text{ kg}^{-1} = \text{permittivity of the vacuum}$

$$oldsymbol{\mathcal{F}_P} = rac{\mathbf{E} imes \mathbf{B}}{\mu_0}$$

 \mathcal{F}_{P} = Poynting vector; W/m² = direction & magnitude of the e.m. wave energy flow

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 $\mu_0 = 4\pi \times 10^{-7}$ T m A⁻¹ = permeability of free space $\epsilon_0 = 8.854 \times 10^{-12}$ s⁴ A² m⁻³ kg⁻¹ = permittivity of the vacuum

$$\mathbf{E}(\mathbf{r},t) = E_{tr}\mathbf{\hat{n}} = \frac{qa(t')sin\theta}{4\pi\epsilon_0 c^2 r}\mathbf{\hat{n}}$$

$$\mathbf{E}(\mathbf{r}, t) = \text{Transverse electric vector; V/m; } v << c$$





$$oldsymbol{\mathcal{F}_P} = rac{\mathbf{E} imes \mathbf{B}}{\mu_0}$$

 \mathcal{F}_{P} = Poynting vector; W/m² = direction & magnitude of the e.m. wave energy flow

$$\mathcal{F}_P(r, heta,t) = rac{q^2 sin^2 heta a^2(t')}{(4\pi)^2 \epsilon_0 c^3 r^2}$$

 $\mathcal{F}_{P}(r, \theta, t) = ext{magnitude of Poynting vector in vacuum } v << c; ext{ W/m}^2$

[for an observer at distance r and angle θ from acceleration direction]





$$oldsymbol{\mathcal{F}_P} = rac{\mathbf{E} imes \mathbf{B}}{\mu_0}$$

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$$\mathcal{F}_P(r,\theta,t) = \frac{q^2 sin^2 \theta a^2(t')}{(4\pi)^2 \epsilon_0 c^3 r^2}$$

 $\mathcal{F}_P(r, \theta, t) = \text{magnitude of Poynting vector in vacuum } v << c; W/m^2$ [for an observer at distance r and angle θ from acceleration direction]

$$\mathcal{P}(t) = \int_{\theta=0}^{\pi} \int_{\phi=0}^{2\pi} \mathcal{F}_P(r,\theta,t) \ r^2 \ \sin\theta \ \mathrm{d}\phi \ \mathrm{d}\theta$$
$$\rightarrow \mathcal{P}(t) = \frac{1}{6\pi\epsilon_0} \frac{q^2 a(t)^2}{c^3}$$





Larmor's formula

- Power (W) radiated by an electron as it accelerates
- It is valid if the radiating electron is not relativistic (v << c)

PART I: AN ELECTRON & AN ION ENERGY RADIATED PER COLLISION



Fig. 5.3: Astrophysics Processes (CUP), © H Bradt 2008

$$\mathbf{a} = rac{\mathbf{F}}{m} = -rac{1}{4\pi\epsilon_0}rac{Ze^2}{r^2m}\mathbf{\hat{r}} \quad (\mathrm{m/s^2})$$

 \mathbf{a} = acceleration experienced by an electron of charge -e and mass m at a distance r from an ion of charge Ze

$$a_{\max} \approx \frac{1}{4\pi\epsilon_0} \frac{Ze^2}{b^2m}$$
 (maximum acceleration of the electron)
 $au_b \approx b/v$ (collision time)

PART I: AN ELECTRON & AN ION ENERGY RADIATED PER COLLISION



$$Q(b,v) = \int_{-\infty}^{+\infty} \mathcal{P}(t) dt = \frac{1}{6\pi\epsilon_0} \frac{e^2}{c^3} \int_{-\infty}^{+\infty} a(t)^2 dt$$

(total energy emitted by the electron during the transit)

$$ightarrow Q(b,v) pprox rac{1}{6\pi\epsilon_0} rac{e^2}{c^3} a_{max}^2 au_b$$

$$\rightarrow Q(b,v) \approx \frac{1}{(4\pi\epsilon_0)^3} \frac{2}{3} \frac{Z^2 e^6}{c^3 m^2 b^3 v} \quad (J/\text{collision})$$

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PART I: AN ELECTRON & AN ION FREQUENCY OF EMITTED RADIATION



Emitted electric vectors in the same direction as the projected acceleration

▷ Acceleration increases & decreases once → Electric vectors go to a maximum and decreases only once → Single pulse of electric vectors

$$\rightarrow \omega = 2\pi\nu \approx 1/\tau_b = v/b$$
$$\rightarrow \nu = \omega/2\pi \approx v/2\pi b$$
$$\rightarrow b \approx v/2\pi\nu$$

 $\rightarrow \mathrm{d}b \approx -v \,\mathrm{d}\nu/2\pi\nu^2$

PART II: MANY ELECTRONS & AN ION Single-Speed Electrons



Fig. 5.4: Astrophysics Processes (CUP), © H Bradt 2008

$$\mathcal{P}_b(b, v) = Q(b, v) n_e v 2\pi b \, \mathrm{d} b \quad (W/\mathrm{ion in } db \mathrm{at } b)$$

 $\mathcal{P}_b(b, v) = \mathrm{power \ coming \ from \ an \ ion \ and \ a \ flux \ of \ electrons \ of \ density \ n_e}$

$$\begin{split} \int_{b_1}^{b_2} \mathcal{P}_b(b,v) \, \mathrm{d}b &= -\int_{\nu_1}^{\nu_2} \mathcal{P}_\nu(\nu,v) \, \mathrm{d}\nu \\ &\to \mathcal{P}_\nu(\nu,v) \, \mathrm{d}\nu \approx \frac{1}{(4\pi\epsilon_0)^3} \frac{8\pi^2}{3} n_e \frac{Z^2 e^6}{c^3 m^2 v} \mathrm{d}\nu \\ &\to \mathcal{P}_\nu(\nu,v) = -\mathcal{P}_b(b,v) \frac{\mathrm{d}b}{\mathrm{d}\nu} \end{split}$$

PART II: MANY ELECTRONS & AN ION Single-Speed Electrons



Fig. 5.4: Astrophysics Processes (CUP), © H Bradt 2008

- Derived equation independent of frequency/impact parameter: more collisions for large b values (bigger annulus), but each emits a lower energy photon compared to smaller b
- Cutoff frequency: the maximum photon energy is limited by electron velocity (hv_{max} < mv²/2)
- ▶ The derived classical result is correct (with the addition of a Gaunt factor, see below) as long as electrons are non-relativistic (kT << m_ec² - T << 6 x 10⁹ K)

PART II: MANY ELECTRONS & AN ION MANY-SPEED ELECTRONS

$$P(\mathbf{v}) = \left(\frac{m}{2\pi kT}\right)^{3/2} e^{\left(-\frac{mv^2}{2kT}\right)} \quad \text{(Maxwell-Boltzmann distribution)}$$

 $P(\mathbf{v}) = \text{probability of finding a particle with vector velocity } \mathbf{v} \text{ per unit 3-D velocity space}$

$$P(v)\mathrm{d}v = P(\mathbf{v}) \ 4\pi v^2 \ \mathrm{d}v$$

P(v) = probability of an electron's having speed v in dv

 $4\pi v^2 \, \mathrm{d}v =$ volume of a shell in velocity space at speed v

$$\langle \mathcal{P}_{\nu}(\nu) \rangle_{ion} = \int_{v_{min}}^{\infty} \mathcal{P}_{\nu}(\nu, v) P(\mathbf{v}) \ 4\pi v^2 \mathrm{d}v \quad (\mathrm{W \ ion^{-1} \ Hz^{-1}})$$

= Power emitted at ν from an ion in a sea of electrons with a Maxwellian-Boltzmann distribution of speed

$$v_{min} = (2h\nu/m)^{1/2}$$

= Minumum velocity an electron can have for emitting an $h\nu$ energy photon

PART III: MANY ELECTRONS & MANY IONS VOLUME EMISSIVITY

Radiation from a plasma that contains n_i ions per unit volume & n_e electrons per unit volume. They have a Maxwell-Boltzmann distribution of speeds

$$j_{\nu}(\nu) \mathrm{d}\nu = n_i \langle \mathcal{P}_{\nu}(\nu) \rangle_{ion} \mathrm{d}\nu$$

 $j_{\nu}(\nu)$ = Power emitted per unit volume per hertz (W m⁻³ Hz⁻¹)

$$\langle \mathcal{P}_{\nu}(\nu) \rangle_{ion} = \int_{v_{min}}^{\infty} \mathcal{P}_{\nu}(\nu, v) P(\mathbf{v}) \ 4\pi v^2 \mathrm{d}v$$

$$\mathcal{P}_{\nu}(\nu, v) \ \mathrm{d}\nu \approx \frac{1}{(4\pi\epsilon_0)^3} \frac{8\pi^2}{3} n_e \frac{Z^2 e^6}{c^3 m^2 v} \mathrm{d}\nu$$

$$P(\mathbf{v}) = \left(\frac{m}{2\pi kT}\right)^{3/2} e^{\left(-\frac{mv^2}{2kT}\right)}$$

$$v_{min} = (2h\nu/m)^{1/2}$$

$$j_{\nu}(\nu) \mathrm{d}\nu = \frac{1}{(4\pi\epsilon_0)^3} \frac{32}{3} \left(\frac{1}{8} \frac{\pi^3}{k m^3}\right) \frac{Z^2 e^6}{c^3} n_e n_i e^{-h\nu/kT} T^{-1/2} \mathrm{d}\nu$$

PART III: MANY ELECTRONS & MANY IONS VOLUME EMISSIVITY

Radiation from a plasma that contains n_i ions per unit volume & n_e electrons per unit volume. They have a Maxwell-Boltzmann distribution of speeds

$$j_{\nu}(\nu)\mathrm{d}\nu = \frac{1}{(4\pi\epsilon_0)^3} \frac{32}{3} \left(\frac{1}{8} \frac{\pi^3}{k m^3}\right)^{1/2} \frac{Z^2 e^6}{c^3} n_e n_i e^{-h\nu/kT} T^{-1/2} \mathrm{d}\nu$$

Correct result (without our approximations)

$$j_{\nu}(\nu) \mathrm{d}\nu = \mathbf{g}(\nu, \mathbf{T}, \mathbf{Z}) \frac{1}{(4\pi\epsilon_0)^3} \frac{32}{3} \left(\frac{\mathbf{2}}{\mathbf{3}} \frac{\pi^3}{k m^3}\right)^{1/2} \frac{Z^2 e^6}{c^3} n_e n_i e^{-h\nu/kT} T^{-1/2} \mathrm{d}\nu$$

 $g(\nu, T, Z) \approx 1$

$$j_{\nu}(\nu) \mathrm{d}\nu = C_1 \ g(\nu, T, Z) \ Z^2 \ n_e n_i \ e^{-h\nu/kT} \ T^{-1/2} \ \mathrm{d}\nu$$

Saturday, October 5, 2013

PART III: MANY ELECTRONS & MANY IONS EXPONENTIAL SPECTRUM

 $g(\nu, T, Z) \approx 1$

 $j_{\nu}(\nu) \mathrm{d}\nu = C_1 \ g(\nu, T, Z) \ Z^2 \ n_e n_i \ e^{-h\nu/kT} \ T^{-1/2} \ \mathrm{d}\nu$



PART III: MANY ELECTRONS & MANY IONS INTEGRATED VOLUME EMISSIVITY

 $g(\nu, T, Z) \approx 1$

 $j_{\nu}(\nu) d\nu = C_1 g(\nu, T, Z) Z^2 n_e n_i e^{-h\nu/kT} T^{-1/2} d\nu$

It can be shown that most of the power from a bremmstrahlung emitting plasma arises in the frequency band near the cutoff (@ $h v \sim k T$)

Integrated volume emissivity

$$j(T) = \int_0^\infty j_\nu(\nu) d\nu = C_2 \ \bar{g}(T, Z) \ Z^2 \ n_e n_i \ T^{1/2} \quad (W/m^3)$$
with
$$C_2 = 1.44 \times 10^{-40} \ W \ m^3 \ K^{-1/2}$$

THERMAL BREMSSTRAHLUNG FINAL EQUATIONS

Volume emissivity of hydrogen plasma:

 $j_{\nu}(\nu,T) \propto g(\nu,T) n_e^2 T^{-1/2} e^{-h\nu/kT} \quad \mathrm{W \ m^{-3} \ Hz^{-1}}$



Fig. 5.1: Astrophysics Processes (CUP), © H Bradt 2008

 $I(\nu,T) \propto g(\nu,T) n_e^2 T^{-1/2} e^{-h\nu/kT} \Lambda ~~{\rm W}~{\rm m}^{-2}~{\rm Hz}^{-1} {\rm sr}^{-1}$

DISCOVERY OF GALAXY CLUSTERS



Most galaxies are not isolated in the Universe. They are bound together by their mutual gravity in structures containing from a few galaxies, to hundreds or even thousands galaxies

«...remarkable collection of many hundreds of <u>nebulae</u> which are to be seen in what I have called the nebulous <u>stratum</u> of Coma Berenices» - W. Herschel (1785)

Rich clusters are the <u>largest gravitationally bound</u> systems in the Universe

They form by merging of units of smaller mass

A VERY SHORT HISTORICAL OVERVIEW OF OPTICAL OBSERVATIONS



→ Discovery of concentration of nebulae (1785)

W. Herschel



 → First statistical significative sample of clusters (1958; 1989)

G.O. Abell



→ Most of the
 observed nebulae
 are other galaxies
 (1925)

E. Hubble



→ Discovery of an unobservable matter in clusters (1933)

F. Zwícky

DOMINANT MASS COMPONENT OF CLUSTERS: DARK MATTER

Equilibrium is maintained by the balance between the potential energy associated with the mass of the system and the kinetic energy of its individual components:

virial equilibrium

$2 E_k + E_p = Vir = 0$



46

The dominant baryonic component of clusters: hot (10⁷-10⁸ K) intracluster medium (ICM)



80 % : dark matter 15 % : hot intracluster gas 3 % : galaxies

Galaxy clusters:

complex astrophysical systems
 complex evolutionary physics

Image Credits: X-ray: NASA/CXC/CfA/M.Markevitch et al.; Optical: NASA/STScI; Magellan/U.Arizona/D.Clowe et al.

Saturday, October 5, 2013





HYDROdynamic Simulations and Kinematic Investigations of the Intra-Cluster Medium

Schindler & collaborators Innsbruck University

EXERCICE

The Orion nebula, an HII region, is radiating by thermal bremmstrahlung. Consider it to be spherical (radius = 8 light years), optically thin, and at a temperature T = 8000 K. Let Z = 1 , g = 1, $n_e = n_i = 6 \times 10^{-8} \text{ m}^{-3}$.

- (a) Find the luminosity (W) of the entire nebula in terms of solar luminosities.
- (b) In what wavelength band orbands will the power from theOrion nebula be radiated ?



IMAGE CREDITS FOR THIS LECTURE

- ▶ H. Bradt, 2008, "Astrophysical processes", Cambridge University Press
- NASA/JPL/Caltech/University of Arizona/Harvard-Smithsonian Center for Astrophysics/NOAO/AURA/NSF
- NASA/ESA/JHU (L. Bradley, H. Ford)/ UCSC (R. Bouwens, G. Illingworth)
- THINGS Survey/Fabian Walter, MPIA/Karl Gordon, Steward Observatory
- NASA/CXC/SAO/A. Vikhlinin; ROSAT; DSS; NSF/NRAO/VLA/IUCAA/J.Bagchi
- ▶ Rau & Cornwell, A&A, 2011, 532, 17
- <u>http://www.plasma.inpe.br/LAP_Portal/LAP_Site/Text/</u> <u>Variety_of_Plasmas.htm</u>